



*First Semester of 2018-1439/1440H Academic Year*

## **Computation Theory Course, 6803415-3**

### **BONUS ASSIGNMENT**

**-Solutions-**

Last Delivery Date: Group One and Two: Sunday, 09 / 04 / 1440 H – 16 / 12 / 2018

#### **Question One: 2 Mark**

Choose the best answer.

1. Which one of the following is not an asymptotic notation for the function:  $f(n) = n^2$ ?

- a)  $O(n)$
- b)  $O(n \log^2 n)$
- c)  $O(\frac{1}{n})$
- d) All of them

2. Which one of the following languages can be generated by the grammar:

$$S \rightarrow 0S0 \mid 0S1 \mid 1S0 \mid 1S1 \mid 0$$

- a)  $L = \{w \mid \text{the length of } w \text{ is odd and its middle is } 0\}$
- b)  $L = \{w \mid \text{the length of } w \text{ is odd}\}$
- c)  $L = \{w \mid w \text{ contains at least 2 1's}\}$
- d) None of the above

3. The language:  $\{0^n 1^n 0^n 1^n \mid n \geq 0\}$  is a context free language.

- a) True
- b) False

4. Is the formula  $(x \vee y) \wedge (x \vee \bar{y}) \wedge (\bar{x} \vee y) \wedge (\bar{x} \vee \bar{y})$  satisfiable?

- a) True
- b) False



**Question Two: 1 Mark**

Show that NP is closed under the star operation.

**Answer of Question Two:**

Let the language  $A \in \text{NP}$ .

By constructing NTM  $L$  to decide  $A^*$  in nondeterministic polynomial time, we can easily proof that NP is closed under the star operation.

$L =$  "On input  $w$ :

1. Nondeterministically divide  $w$  into pieces  $w = x_1x_2 \cdot \dots \cdot x_k$ .
2. For each  $x_i$ , nondeterministically guess the certificates that show  $x_i \in A$ .
3. Verify all certificates if possible, then accept.  
Otherwise, if verification fails, reject."

Remember, "*Success is 1% inspiration and 99% perspiration*" 😊

If you have any questions, feel free to ask me through my email

T.Mariah Sami Ahmed Khayat

Teacher Assistant @ Adam University College

[mskhayat@uqu.edu.sa](mailto:mskhayat@uqu.edu.sa)